# Multi dimensional scaling of geomagnetic Sq (H) variations 

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#### Abstract

The dominant relationship in respect of geomagnetic solar quiet day variations (Sq) among the six Indian geomagnetic observatories is analysed by employing multidimensional scaling. This is a powerful technique for data analysis to identify the proximity and dominance relationship between data points of different classes.


Keywords: Multidimensional scaling, Proximity relationship, Geomagnetic solar quiet day ( Sq ) variation
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## 1 Introduction

The extent to which the high and low latitude ionosphere is interlinked electromagnetically during quiet geomagnetic conditions is a point of debate. This paper aims to give a quantitative estimation in terms of proximity distance of geomagnetic solar quiet day ( Sq ) variation ranges of the horizontal H component which is highly sensitive to the ionospheric dynamo current. The technique of multidimensional scaling (MDS) is applied to find the proximity relationship. Proximity relationship in MDS reveals the similarity or dissimilarity between the entities to which the indices differ. The superiority of MDS over the conventional correlation coefficient method to establish internal relationship of several data points of different classes has been proved by Sridharan \& Ramasamy ${ }^{1}$ for the analysis of geomagnetic storms and hence the same process is not repeated here. The aim of this technique is simplification and reduction of data structures and rescaling of original data into new and reduced space so that patterns and relationship of original objects can be conveniently examined in a two-dimensional plot. The daily variation in the magnetic field at the earth's surface during geomagnetic quiet periods (Sq) is known to be associated with the dynamo currents driven by winds and tidal motions in the E-region of the ionosphere known as atmospheric dynamo. Besides the atmospheric dynamo, other sources of electric field and currents at equatorial region contribute to Sq variations on different components of geomagnetic fields observed at the ground level ${ }^{2}$.

Daily range of the geomagnetic field is an important parameter measuring the magnitude of diurnal variation. Being dependent on the daily maximum and minimum field values, the parameter fluctuates from day to day in accordance with the variability of both these values. Internationally declared geomagnetic quiet days data are considered for this analysis. For each day of a calendar month, every three hours, the order numbers $(\mathrm{Kp})$ are assigned on the basis of the level of geomagnetic activity. Days with the five lowest mean order numbers are chosen as quiet days and those with five highest values as the excessively disturbed days of the month. On days not excessively disturbed, the daily maximum should be predominantly controlled by ionospheric dynamo Sq current intensity, so that the daily range and maximum values may be expected to fluctuate in unison. The unique configuration of the ionosphere over the equatorial region can contribute significantly in judging the nature of the effect ${ }^{3}$. The daily range of $\mathrm{Sq}(\mathrm{H})$ variation has been studied to reveal the annual variation and seasonal changes at Alibag ${ }^{4}$. Quantitative estimation of the contribution to the day to day variability of Sq current and equatorial electrojet has been studied by Alex et al. ${ }^{5}$ Rangarajan et al. ${ }^{6}$ found that disturbance dynamo caused by even moderate geomagnetic activity alters the shape and structure of the equatorial electrojet and Sq current system. Absence of equatorial enhancement in annual periodicity was observed in monthly ranges of $\mathrm{Sq}(\mathrm{H})$ variations by $\mathrm{Yacob}^{7}$. Simultaneous data of six Indian geomagnetic observatories during January 1996-

September 1999 are considered for this analysis. Analytical technique and the result of the analysis are presented in this paper.

## 2 Multidimensional scaling technique

Multidimensional scaling moves objects around the space defined by the requested number of dimensions, and checks how well the distances between objects can be reproduced by the new configuration. It uses a function minimization that evaluates different configurations with the goal of maximizing the goodness-of-fit or minimizing lack of fit. It is complementary with classical factor analysis. In factor analysis, the similarities or dissimilarities between objects are expressed in the correlation matrix. In MDS, one may analyze any kind of similarity or dissimilarity matrix, in addition to correlation matrices. The actual orientation of axes in the final solution is arbitrary; the dimensions of such a configuration can be freely translated, permuted, reflected, orthogonally rotated and uniformly rescaled to facilitate the interpretation. The final orientation of axes in the plane or space is mostly the result of a subjective decision by the researcher, who will choose an orientation that can be most easily explained.

One classical example of multi dimensional scaling is the judgment of efficiency of a particular dispensary or a hospital in a location based on the data of several treatments for a number of diseases by different physicians during different periods in comparison with similar data at various places in other locations. For a background of this technique, one may refer models and methods for multidimensional analysis of preferential choice by Carrol ${ }^{8}$, Armitage \& Cotton ${ }^{9}$ and Thompson \& Woodbury ${ }^{10}$. In this paper, multidimensional reduction technique ${ }^{1}$ is applied to identify the proximity relationship of Indian observatories in respect of the variations in the horizontal (H) component of the geomagnetic field during international quiet days.

## 3 Analytical technique

For the purpose of analysis of data, H field range of every month from January 1996 to September 1999 was represented as points in a multidimensional space of which one dimension was allocated for each of the six stations. It is not possible to visualize geometrically such a higher dimensional space for the purpose of understanding the concept of representation of Sq variations by means of points in
that space. However, it may be mentioned that just as one can compute the distance between two points in a two-dimensional plane or in a three-dimensional space, the distance in an n-dimensional Euclidean space between two points with coordinates ( $\mathrm{X}_{11}, \mathrm{X}_{12}$, .., $\mathrm{X}_{1 \mathrm{n}}$ ) and ( $\mathrm{X}_{21}, \mathrm{X}_{22}, \ldots, \mathrm{X}_{2 \mathrm{n}}$ ) can be calculated from the following well known formula:

$$
\begin{align*}
\mathrm{D} & =\text { Square root of }\left[\left(\mathrm{X}_{11}-\mathrm{X}_{21}\right)^{2}\right. \\
& \left.+\left(\mathrm{X}_{12}-\mathrm{X}_{22}\right)^{2}+\ldots+\left(\mathrm{X}_{1 \mathrm{n}}-\mathrm{X}_{2 \mathrm{n}}\right)^{2}\right] \tag{1}
\end{align*}
$$

This distance is a number, which tends to be small if the values of the corresponding coordinates of the two points are similar in magnitude and large if the points differ significantly in several coordinates. Therefore, the computed distance between two points can be used as a measure of similarity or dissimilarity between the Sq ranges of two months at two given points at a time. If a series of points represent the sequence of Sq variation of a single station in time, the path or trajectory connecting the point is indicative of the station's Sq variation.

Using Eq. (1), distances between one point and all other variable points in the $n$-dimensional space can be computed. Spanning distance of a month with respect to other 44 months is found. Next, the distances are ranked in ascending order. This enables one to find out which point is closest to which other point, the second closest point and so on. A minimum coverage algorithm is employed to connect each point to at least one nearest neighbour. This enables one to construct a branching network that ties together all the available points. Since a tree has no cycles, one has to avoid cycles in the construction of a network. If only points are connected which in some previous steps have not been connected to the same network; the final network will be a tree. It is not really possible to display accurately an n-dimensional network on a two dimensional plane. However, by stretching, bending and twisting the arcs connecting adjacent points, it is usually possible to locate the points on a plane, so that most of the near neighbours of each point are closer to it, while points which are not its neighbours tend to be farther away. The resulting "road map" provided is at best an approximation of the real situation but still it may contain a surprising amount of useful information in a highly compressed form.

## 4 Dimension reduction technique

The way in which points in n-dimensional space have been connected by a tree will be maintained for the further process.

Now, instead of n coordinates, choose any two coordinates and determine the distances between the points as restricted to these two coordinates. The sum of the distances is calculated. This sum gives the covering distance for all the points in the graph, in the two dimensional sense. This procedure is repeated for each pair of coordinates in the n -dimensional space. For each pair of coordinates, consider the tree structure and the corresponding covering distance in the two dimensional sense. One will have $n(n-1) / 2$ values of such covering distances. The covering distances for all possible trees are put in ascending order. With the help of this ordering one can find out which two factors are approximately nearby compared to the remaining factors in the two dimensional sense. Nearness of two points in the two dimensional sense does not mean that they are geographically nearby. But it indicates that they possess almost similar characteristics with respect to a certain feature.

## 5 Data analysis

The geographic and dipole coordinates of the observatories are presented in Table 1. From 1996 to 1999, there were 240 international quiet days. Since Trivandrum observatory was closed in September 1999 due to technical reasons, simultaneous data for six observatories, viz. Alibag, Nagpur, Pondicherry, Trivandrum, Ujjain and Visakapatnam are considered for 225 international quiet days. The daily ranges, that is, the difference between daily maximum and minimum ${ }^{11}$ are found and their monthly average is calculated and presented in Table 2.

Monthly mean values of geomagnetic Sq ranges, presented in Table 2, are used to find 990 proximity distances presented in Table 3. The distances are calculated by applying Eq. (1). Proximity relationship, in respect of 45 months from Jan 1996 to Sep 1999 derived from Table 3, is used to derive pair of months presented in Table 4. It is derived by taking only least 44 values among 990 values as described in the analytical technique.

The pair of months (period) presented in Table 4 are used to construct a tree structure provided in Fig. 1. Proximity distances between a pair of stations with respect to pair of months are again found using the Eq. (1) and is presented in Table 4. The sum of total covering distances described in Table 4 is applied to construct the tree described in Fig. 2. Only the highlighted minimum distances (sum) were taken for getting the tree structure as described in dimension reduction technique.

## 6 Results

It is observed from Fig. 2 that Alibag Visakhapatnam observatories are very close to each other in terms of solar quiet (Sq) day variations and Alibag - Trivandrum observatories are at the extreme end. Trivandrum is close to the magnetic equator. The unique condition of orthogonality of electric field, magnetic field and plasma density gradient in the Eregion over the magnetic equator makes this region very sensitive to the changes of electric fields. The normal eastward electric field during day time causes a strong eastward current-equatorial electrojet (EEJ). The abnormal features of Sq variations have been studied by scientists and the day-to-day changes in the electrojet strengths have been estimated by the difference field $(\Delta \mathrm{H})$ of daily variations of Alibag and Trivandrum ${ }^{5}$. The Sq variation at Pondicherry is similar to Nagpur and it is not influenced by EEJ effect, is confirmed by a dendogram on the analysis of fuzzy clustering to study geomagnetic coastal effects ${ }^{12}$. One can observe that the spanning distance between Pondicherry and Trivandrum is larger than Pondicherry and Nagpur. Though Pondicherry is geographically close to Trivandrum, the range of Sq $(\mathrm{H})$ variation between the two places is larger, whereas geographically far away places at Nagpur and Pondicherry, Sq variation is similar. This confirms that Pondicherry is not influenced by the day time equatorial electrojet.

| Table 1—Location of Observatories (geographic and dipole coordinates) and its abbreviations |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| S. No | Station | Geographic |  | Dipole |  |
|  |  | Latitude | Longitude | Latitude | Longitude |
|  |  |  |  |  |  |
| 1 | Alibag (ALB) | $18^{\circ} 37^{\prime} \mathrm{N}$ | $72^{\circ} 52^{\circ} \mathrm{E}$ | $10.0^{\circ} \mathrm{N}$ | $145.9^{\circ}$ |
| 2 | Nagpur (NAG) | $21^{\circ} 09^{\prime} \mathrm{N}$ | $79^{\circ} 05^{\prime} \mathrm{E}$ | $11.9^{\circ} \mathrm{N}$ | $152.1^{\circ}$ |
| 3 | Pondicherry (PON) | $11^{\circ} 55^{\prime} \mathrm{N}$ | $79^{\circ} 55^{\prime} \mathrm{E}$ | $2.7^{\circ} \mathrm{N}$ | $152.1^{\circ}$ |
| 4 | Trivandrum (TRV) | $08^{\circ} 29^{\prime} \mathrm{N}$ | $76^{\circ} 58^{\prime} \mathrm{E}$ | $07.8^{\circ} \mathrm{N}$ | $155.5^{\circ}$ |
| 5 | Ujjain (UJJ) | $23^{\circ} 11^{\prime} \mathrm{N}$ | $75^{\circ} 47^{\prime} \mathrm{E}$ | $14.3^{\circ} \mathrm{N}$ | $149.2^{\circ}$ |
| 6 | Visakhapatnam (VIZ) | $17^{\circ} 41^{\prime} \mathrm{N}$ | $83^{\circ} 19^{\prime} \mathrm{E}$ | $08.2^{\circ} \mathrm{N}$ | $155.9^{\circ}$ |


| Table 2-Monthly Sq (H) ranges from January 1996 to September 1999 |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| S. No. | Month | ALI | NAG | PON | TRV | UJJ | VSK |
| 1 | Jan 1996 | 31.6 | 36.6 | 42.6 | 65.2 | 21 | 33.2 |
| 2 | Feb 1996 | 41.8 | 50 | 49.4 | 63.4 | 33 | 44.8 |
| 3 | Mar 1996 | 38 | 60 | 47.4 | 76 | 33.4 | 43.4 |
| 4 | Apr 1996 | 41.8 | 51.4 | 65 | 99.8 | 34.2 | 51 |
| 5 | May 1996 | 41.8 | 50.2 | 49 | 68.8 | 36.2 | 44.4 |
| 6 | Jun 1996 | 42.8 | 48.4 | 45 | 72.6 | 37.6 | 42 |
| 7 | Jul 1996 | 28.8 | 46.4 | 38.2 | 73.4 | 25.2 | 28.4 |
| 8 | Aug 1996 | 24.6 | 47.4 | 40.2 | 80.8 | 25.6 | 24.6 |
| 9 | Sep 1996 | 38.4 | 36.4 | 58.6 | 95.4 | 27.2 | 41.4 |
| 10 | Oct 1996 | 40.4 | 53.2 | 53.2 | 84.2 | 35.6 | 45.6 |
| 11 | Nov 1996 | 42.4 | 52.2 | 46.4 | 57 | 34.8 | 43.4 |
| 12 | Dec 1996 | 28 | 46.8 | 35 | 58.8 | 21.6 | 29.2 |
| 13 | Jan 1997 | 24.6 | 40.8 | 34.4 | 60.4 | 17.8 | 24.8 |
| 14 | Feb 1997 | 36.4 | 46 | 43.4 | 62.4 | 27.8 | 37.2 |
| 15 | Mar 1997 | 46.8 | 63.4 | 60.2 | 100.2 | 36 | 50.2 |
| 16 | Apr 1997 | 32.2 | 54 | 51.4 | 92 | 24 | 34.8 |
| 17 | May 1997 | 34.6 | 49.8 | 47.2 | 79.4 | 28 | 36.4 |
| 18 | Jun 1997 | 38.6 | 53 | 49.2 | 80.2 | 28 | 42.6 |
| 19 | Jul 1997 | 39 | 44.2 | 40 | 64 | 34 | 32.8 |
| 20 | Aug 1997 | 39.8 | 62.8 | 48.4 | 82.4 | 34.8 | 39.6 |
| 21 | Sep 1997 | 39 | 45.4 | 60.4 | 112.2 | 32.6 | 43.8 |
| 22 | Oct 1997 | 34.2 | 45.2 | 60.4 | 110.4 | 23.6 | 41.8 |
| 23 | Nov 1997 | 39.8 | 60.2 | 52.4 | 86.6 | 30.2 | 45.4 |
| 24 | Dec 1997 | 21 | 28.8 | 32 | 54.4 | 16 | 23.4 |
| 25 | Jan 1998 | 29.2 | 55.2 | 42.6 | 64.4 | 23.2 | 34.4 |
| 26 | Feb 1998 | 35.6 | 49.8 | 46.6 | 81.4 | 28 | 39.4 |
| 27 | Mar 1998 | 45.6 | 60.8 | 58.6 | 105.8 | 38.2 | 53 |
| 28 | Apr 1998 | 52 | 53 | 76.6 | 140.2 | 45.2 | 59.6 |
| 29 | May 1998 | 45 | 57.4 | 56 | 95.8 | 39.6 | 50.2 |
| 30 | Jun 1998 | 42.2 | 62.4 | 42 | 65 | 37.6 | 43.6 |
| 31 | Jul 1998 | 41.6 | 66.8 | 39.6 | 76.2 | 35 | 44.4 |
| 32 | Aug 1998 | 50.2 | 65.4 | 49.8 | 83 | 40.6 | 49.2 |
| 33 | Sep 1998 | 48.8 | 52.6 | 58.8 | 126.8 | 38.6 | 58 |
| 34 | Oct 1998 | 44.2 | 60.4 | 68.6 | 119.4 | 28.8 | 53.4 |
| 35 | Nov 1998 | 56.8 | 67 | 59 | 90 | 43.4 | 56.2 |
| 36 | Dec 1998 | 29 | 45.6 | 39 | 90.8 | 17.4 | 31.4 |
| 37 | Jan 1999 | 45.6 | 56.6 | 53.6 | 92.8 | 31.8 | 50 |
| 38 | Feb 1999 | 43.4 | 54 | 55.8 | 98.8 | 29.4 | 48.4 |
| 39 | Mar 1999 | 56.8 | 67 | 86.4 | 126.4 | 40.8 | 61.6 |
| 40 | Apr 1999 | 53.2 | 71.6 | 62.6 | 113.8 | 41.6 | 58.2 |
| 41 | May 1999 | 58.6 | 79.4 | 62.2 | 102.2 | 47 | 60.2 |
| 42 | Jun 1999 | 72.4 | 79.4 | 69.2 | 85.8 | 56.8 | 69.8 |
| 43 | Jul 1999 | 69.2 | 73.2 | 79.8 | 126.2 | 51.2 | 68.2 |
| 44 | Aug 1999 | 58.8 | 68.4 | 65.6 | 109.4 | 45 | 60 |
| 45 | Sep 1999 | 60.6 | 75.6 | 75.6 | 141.2 | 45.8 | 62 |


| Table 3-Spanning distances of 45 months from January 1996 to September 1999 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 1 | 611.6 | 986 | 2513 | 699.4 | 678.2 | 231.2 | 509.9 | 1320 | 1193 | 736.2 | 232.1 | 237.7 | 182.1 | 2998 | 1110 |
| 2 |  | 279.3 | 1610 | 39.76 | 136.6 | 737.2 | 1153 | 1350 | 466.7 | 60.4 | 802.5 | 1246 | 167 | 1714 | 1111 |
| 3 |  |  | 1023 | 173.7 | 194.5 | 653.2 | 827.5 | 1101 | 162.5 | 444.2 | 1065 | 1550 | 469.3 | 891.5 | 503.9 |
| 4 |  |  |  | 1266 | 1242 | 2201 | 2059 | 438 | 418.9 | 2237 | 3427 | 3852 | 2155 | 196.1 | 711.2 |
| 5 |  |  |  |  | 42.4 | 698.2 | 1030 | 1092 | 267.6 | 153.3 | 942.2 | 1391 | 241.5 | 1344 | 891.6 |
| 6 |  |  |  |  |  | 585.6 | 869.3 | 976.7 | 247.5 | 269.7 | 931.9 | 1338 | 272.4 | 1304 | 797.8 |
| 7 |  |  |  |  |  |  | 92 | 1265 | 926.4 | 872 | 237.8 | 300 | 290.2 | 2407 | 632 |
| 8 |  |  |  |  |  |  |  | 1148 | 1005 | 1383 | 560.1 | 554.2 | 653.6 | 2289 | 458.8 |
| 9 |  |  |  |  |  |  |  |  | 529 | 1951 | 2293 | 2384 | 1434 | 980 | 465.4 |
| 10 |  |  |  |  |  |  |  |  |  | 7965 | 1636 | 2073 | 770.5 | 471.3 | 383.1 |
| 11 |  |  |  |  |  |  |  |  |  |  | 745.6 | 1237 | 200 | 2249 | 1548 |
| 12 |  |  |  |  |  |  |  |  |  |  |  | 84.3 | 257 | 3626 | 1478 |
| 13 |  |  |  |  |  |  |  |  |  |  |  |  | 505 | 4230 | 1658 |
| 14 |  |  |  |  |  |  |  |  |  |  |  |  |  | 2358 | 1042 |
| 15 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 827.4 |
|  | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 |
| 1 | 465.3 | 723.9 | 289.9 | 1315 | 2905 | 2521 | 1412 | 523.2 | 358.6 | 556.1 | 3374 | 8748 | 2363 | 1162 | 1464 |
| 2 | 408.3 | 331.4 | 275.2 | 560.1 | 2533 | 2508 | 663.5 | 2013 | 437.2 | 424.5 | 2108 | 7119 | 1231 | 233.8 | 546.3 |
| 3 | 205.3 | 100 | 562.1 | 69.4 | 1694 | 1684 | 154.9 | 2669 | 443.1 | 184.7 | 1187 | 5621 | 606.4 | 191.2 | 123.6 |
| 4 | 1039 | 755.6 | 2298 | 842.6 | 273.2 | 426.7 | 461.8 | 5187 | 2325 | 891.1 | 199.8 | 2068 | 173 | 1928 | 1484 |
| 5 | 298.8 | 218.5 | 287.3 | 373.1 | 2058 | 2109 | 469.4 | 2236 | 513.1 | 295.4 | 1666 | 6284 | 885.3 | 215 | 420.2 |
| 6 | 243.8 | 206.7 | 228.6 | 337.5 | 1857 | 1946 | 465.3 | 2172 | 569.3 | 232.7 | 1570 | 6042 | 816.3 | 265.7 | 394.6 |
| 7 | 234 | 516.3 | 297.3 | 792.6 | 2395 | 2075 | 1001 | 879.7 | 218 | 321 | 2730 | 7892 | 1885 | 905.4 | 941.8 |
| 8 | 301.7 | 638.5 | 637.7 | 847.6 | 2023 | 1681 | 1031 | 1217 | 458.5 | 393 | 2549 | 7245 | 1842 | 1293 | 1167 |
| 9 | 605.6 | 597 | 1513 | 1033 | 401.7 | 336.4 | 709.3 | 3199 | 1721 | 532 | 1011 | 3447 | 722.7 | 2003 | 1734 |
| 10 | 246.6 | 102 | 831.6 | 155.4 | 911 | 999.2 | 85 | 3186 | 913 | 182.2 | 642 | 4106 | 218.3 | 590 | 437.2 |
| 11 | 664.2 | 608 | 278.5 | 783 | 3306 | 3292 | 1008 | 1973 | 468 | 710 | 2718 | 8298 | 1701 | 195 | 629.7 |
| 12 | 718.6 | 1031 | 346.5 | 1414 | 3954 | 3512 | 1731 | 466.4 | 190.7 | 857.1 | 4114 | 10452 | 2976 | 996 | 1320 |
| 13 | 944.4 | 1376 | 589.7 | 1903 | 4168 | 3610 | 2196 | 204 | 433 | 1109 | 4699 | 11010 | 3532 | 1601 | 1922 |
| 14 | 322 | 433.5 | 82 | 774 | 2843 | 2637 | 953 | 1057 | 170 | 391 | 2776 | 8252 | 1787 | 448.3 | 768 |
| 15 | 1190 | 818.2 | 2455 | 619.2 | 581.4 | 818.4 | 361.7 | 5874 | 2382 | 1029 | 55 | 2177 | 89.2 | 1639 | 1074 |
| 16 | 218.4 | 263 | 1160 | 376 | 764.2 | 550 | 277.2 | 2745 | 850.4 | 201.8 | 1001 | 4416 | 691.5 | 1250 | 854 |
| 17 |  | 69.3 | 389 | 263 | 1365 | 1205 | 300 | 1795 | 332 | 14.4 | 1449 | 5708 | 837 | 595 | 519 |
| 18 |  |  | 557 | 158 | 1230 | 1138 | 117.2 | 2370 | 476.7 | 37.7 | 1066 | 5115 | 542.2 | 477.4 | 359.8 |
| 19 |  |  |  | 802.6 | 2864 | 2782 | 1094 | 1130 | 343.2 | 468.8 | 2838 | 8236 | 1812 | 476.1 | 802 |
| 20 |  |  |  |  | 1358 | 1399 | 95.2 | 3178 | 689.4 | 237.2 | 880.4 | 4889 | 428.9 | 373.5 | 158.2 |
| 21 |  |  |  |  |  | 111.3 | 947.4 | 5439 | 2971 | 1211 | 440.9 | 1682 | 558.3 | 2891 | 2200 |
| 22 |  |  |  |  |  |  | 943.3 | 4782 | 2613 | 1080 | 736.3 | 2312 | 824.5 | 2959 | 2260 |
| 23 |  |  |  |  |  |  |  | 3478 | 896.2 | 227.3 | 562.8 | 4086 | 243.9 | 643.3 | 342.8 |
| 24 |  |  |  |  |  |  |  |  | 1149 | 1996 | 6348 | 13061 | 4959 | 2665 | 3203 |
| 25 |  |  |  |  |  |  |  |  |  | 423.2 | 2841 | 8545 | 1939 | 513.5 | 675.8 |
| 26 |  |  |  |  |  |  |  |  |  |  | 1249 | 5341 | 693 | 602.2 | 475 |
| 27 |  |  |  |  |  |  |  |  |  |  |  | 1702 | 128.5 | 2043 | 1373 |
| 28 |  |  |  |  |  |  |  |  |  |  |  |  | 2584 | 7350 | 6099 |
| 29 |  |  |  |  |  |  |  |  |  |  |  |  |  | 1225 | 807.8 |
| 30 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 158.3 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | Contd. |

Table 3—Spanning distances of 45 months from January 1996 to September 1999—Contd.

|  | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2184 | 5534 | 4808 | 3474 | 772.3 | 1878 | 2047 | 8422 | 5503 | 5719 | 7250 | 9995 | 5528 | 10672 |
| 2 | 769.2 | 4369 | 3710 | 1552 | 1465 | 968.5 | 1339 | 6195 | 3564 | 3249 | 3886 | 7036 | 3381 | 8208 |
| 3 | 318.2 | 3122 | 2493 | 996.8 | 978 | 436.1 | 696.5 | 4849 | 2312 | 2173 | 3376 | 5649 | 2360 | 6300 |
| 4 | 824 | 886.4 | 518.8 | 712.1 | 1621 | 227.2 | 124.8 | 1790 | 846.4 | 1328 | 2798 | 2727 | 868.2 | 3021 |
| 5 | 546.3 | 3706 | 3190 | 1248 | 1291 | 703.3 | 1026 | 5541 | 3018 | 2791 | 3556 | 6315 | 2865 | 7350 |
| 6 | 535.8 | 3439 | 3101 | 1276 | 1086 | 654.7 | 943 | 5545 | 2932 | 2802 | 3739 | 6267 | 2813 | 7166 |
| 7 | 1716 | 4770 | 4111 | 3021 | 374 | 1510 | 1644 | 7686 | 4615 | 4869 | 6817 | 9129 | 4821 | 9413 |
| 8 | 1907 | 4359 | 3689 | 3175 | 237.5 | 1533 | 1545 | 7235 | 4379 | 4847 | 7191 | 8840 | 4703 | 8799 |
| 9 | 1452 | 1762 | 1432 | 1786 | 774.3 | 586.7 | 408 | 3602 | 2302 | 3062 | 4892 | 4995 | 2348 | 5186 |
| 10 | 296 | 2080 | 1650 | 700 | 965.8 | 146.5 | 276 | 3626 | 1662 | 1766 | 3004 | 4455 | 1654 | 5034 |
| 11 | 990 | 5295 | 4593 | 1912 | 1867 | 1416 | 1894 | 7210 | 4245 | 3726 | 4170 | 7948 | 4025 | 9288 |
| 12 | 2405 | 6775 | 5886 | 3992 | 1065 | 2444 | 2751 | 9868 | 6278 | 6229 | 7820 | 11341 | 6408 | 11992 |
| 13 | 3124 | 7264 | 10358 | 4846 | 1031 | 2940 | 3152 | 10667 | 7095 | 7272 | 9177 | 12429 | 7285 | 12901 |
| 14 | 1340 | 5131 | 4416 | 2467 | 1023 | 1405 | 1720 | 7567 | 4580 | 4444 | 5529 | 8720 | 4521 | 9647 |
| 15 | 441.7 | 898 | 517 | 309.2 | 1871 | 163.7 | 168 | 1639 | 394.3 | 624.2 | 2017 | 2213 | 460 | 2493 |
| 16 | 1020 | 2295 | 1601 | 1670 | 291 | 484 | 405 | 4183 | 2209 | 2737 | 4917 | 5569 | 2495 | 5495 |
| 17 | 829 | 3170 | 2552 | 1670 | 384 | 587.2 | 691.4 | 5333 | 2902 | 3124 | 4775 | 6547 | 3016 | 6940 |
| 18 | 498.8 | 2717 | 216.4 | 1141 | 601.1 | 309.3 | 449.2 | 4570 | 2296 | 2421 | 3840 | 5590 | 2359 | 6106 |
| 19 | 1344 | 5120 | 4628 | 2510 | 1099 | 1512 | 1841 | 7759 | 4646 | 4495 | 5571 | 8755 | 4555 | 9672 |
| 20 | 243 | 2618 | 2029 | 826.3 | 941.4 | 324.4 | 520.7 | 4207 | 1837 | 1785 | 3179 | 4964 | 1937 | 5417 |
| 21 | 1584 | 601.2 | 477.7 | 1549 | 1401 | 630.7 | 325.4 | 2045 | 1184 | 2120 | 4308 | 3199 | 1372 | 2956 |
| 22 | 1871 | 1027 | 640.9 | 2004 | 1016 | 750.4 | 395 | 2606 | 1667 | 2722 | 5198 | 4094 | 1961 | 3702 |
| 23 | 277.5 | 2025 | 1424 | 681.2 | 886.8 | 110.2 | 221.4 | 3450 | 1447 | 1563 | 3017 | 4313 | 1555 | 4708 |
| 24 | 4598 | 9007 | 8165 | 6564 | 1786 | 4276 | 4479 | 12959 | 9200 | 9486 | 11390 | 14981 | 9332 | 15572 |
| 25 | 1465 | 5341 | 4345 | 2709 | 844.7 | 1516 | 1795 | 7713 | 4590 | 4495 | 6000 | 9054 | 4735 | 9662 |
| 26 | 724.1 | 2850 | 2311 | 1492 | 383.7 | 452 | 548.8 | 5011 | 2629 | 2875 | 4514 | 6154 | 2743 | 6535 |
| 27 | 659.8 | 543.7 | 375.6 | 451 | 2015 | 261.6 | 206.5 | 1442 | 293 | 670.2 | 2205 | 1976 | 389.2 | 2125 |
| 28 | 4276 | 553 | 919.6 | 3064 | 6006 | 3101 | 2597 | 528.9 | 1255 | 2396 | 4366 | 1020 | 1353 | 592.8 |
| 29 | 295.3 | 1068 | 852.2 | 324.5 | 1556 | 76.6 | 130.4 | 2223 | 704.4 | 903.1 | 2189 | 2784 | 713.7 | 3198 |
| 30 | 498.2 | 4449 | 3848 | 1341 | 1688 | 1027 | 1495 | 6310 | 3241 | 2714 | 3429 | 6810 | 3164 | 7854 |
| 31 | 280.6 | 3380 | 2874 | 1008 | 1301 | 633.2 | 987.6 | 5271 | 2334 | 2028 | 3196 | 5748 | 2420 | 6386 |
| 32 |  | 2247 | 1896 | 236.6 | 1874 | 287.2 | 587.9 | 3423 | 1242 | 950.9 | 1760 | 3661 | 1166 | 4456 |
| 33 |  |  | 350 | 1652 | 3286 | 1320 | 1001 | 1051 | 572.8 | 1506 | 3535 | 1545 | 743.6 | 1226 |
| 34 |  |  |  | 1380 | 2758 | 969.5 | 655.2 | 779.4 | 460.7 | 1283 | 3339 | 1681 | 692.2 | 1387 |
| 35 |  |  |  |  | 2923 | 443.6 | 693.1 | 2112 | 620.7 | 345 | 883.3 | 2140 | 442.9 | 3025 |
| 36 |  |  |  |  |  | 1167 | 1057 | 6205 | 3652 | 4392 | 6990 | 7792 | 4041 | 7521 |
| 37 |  |  |  |  |  |  | 60.8 | 2654 | 968 | 1186 | 2548 | 3342 | 1007 | 3753 |
| 38 |  |  |  |  |  |  |  | 2351 | 921.9 | 1378 | 3043 | 3228 | 1031 | 3406 |
| 39 |  |  |  |  |  |  |  |  | 771.5 | 1369 | 2665 | 387.5 | 747.8 | 449.2 |
| 40 |  |  |  |  |  |  |  |  |  | 257.9 | 1623 | 900.3 | 84.7 | 1023 |
| 41 |  |  |  |  |  |  |  |  |  |  | 696.6 | 1118 | 188.5 | 1724 |
| 42 |  |  |  |  |  |  |  |  |  |  |  | 1827 | 1111 | 3446 |
| 43 |  |  |  |  |  |  |  |  |  |  |  |  | 720.8 | 390 |
| 44 |  |  |  |  |  |  |  |  |  |  |  |  |  | 1171 |

Table 4-Spanning distances of 45 months in two dimensional sense

| Period (Sl. Nos) | $\begin{aligned} & \text { ALB- } \\ & \text { NAG } \end{aligned}$ | $\begin{aligned} & \text { ALB- } \\ & \text { PON } \end{aligned}$ | ALBTRV | $\begin{aligned} & \text { ALB- } \\ & \text { UJJ } \end{aligned}$ | $\begin{aligned} & \text { ALB- } \\ & \text { VSK } \end{aligned}$ | NAGPON | NAGTRV | NAG- <br> UJJ | $\begin{aligned} & \text { NAG- } \\ & \text { VSK } \end{aligned}$ | PON- <br> TRV | PON- <br> UJJ | PON- <br> VSK | TRV- <br> UJJ | TRVVSK | $\begin{aligned} & \text { UJJ- } \\ & \text { VSK } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 17.26 | 1 | 1.17 | 2.24 | 1 | 3.16 | 0.6 | 2 | 0 | 3 | 2.09 | 0.6 | 3.06 | 2 | 3.61 | 3 |
| 26.16 | 5.4 | 5.88 | 11.13 | 5.25 | 5.72 | 6.38 | 11.4 | 5.8 | 6.23 | 11.64 | 6.25 | 6.65 | 11.33 | 11.56 | 6.1 |
| 26.18 | 4.39 | 3.97 | 3.23 | 3 | 4.39 | 4.12 | 3.42 | 3.2 | 4.53 | 2.86 | 2.6 | 4.12 | 1.2 | 3.42 | 3.2 |
| 18.34 | 9.28 | 20.19 | 39.6 | 14.71 | 12.17 | 20.76 | 39.89 | 7.44 | 13.09 | 43.74 | 19.42 | 22.2 | 39.21 | 40.66 | 10.83 |
| 34.33 | 9.06 | 10.83 | 8.71 | 10.83 | 6.51 | 12.53 | 10.75 | 12.53 | 9.06 | 12.28 | 13.86 | 10.83 | 12.28 | 8.71 | 10.83 |
| 33.45 | 25.85 | 20.53 | 18.62 | 13.82 | 12.46 | 28.48 | 27.14 | 24.1 | 23.35 | 22.13 | 18.28 | 17.27 | 16.1 | 14.95 | 8.24 |
| 45.4 | 9.4 | 14.96 | 28.38 | 8.51 | 8.32 | 13.6 | 27.69 | 5.8 | 5.52 | 30.33 | 13.66 | 13.54 | 27.54 | 27.66 | 5.66 |
| 40.44 | 6.45 | 6.35 | 7.12 | 6.55 | 5.88 | 4.39 | 5.44 | 4.67 | 3.67 | 5.33 | 4.53 | 3.5 | 5.56 | 4.75 | 3.85 |
| 44.41 | 11 | 3.41 | 7.2 | 2.01 | 0.28 | 11.51 | 13.15 | 11.18 | 11 | 7.96 | 3.94 | 3.41 | 7.47 | 7.2 | 2.01 |
| 41.42 | 13.8 | 15.47 | 21.43 | 16.93 | 16.81 | 7 | 16.4 | 9.8 | 9.6 | 17.83 | 12.04 | 11.88 | 19.1 | 19 | 13.72 |
| 45.43 | 8.93 | 9.57 | 17.29 | 10.15 | 10.6 | 4.84 | 15.19 | 5.91 | 6.65 | 15.58 | 6.84 | 7.49 | 15.94 | 16.23 | 8.22 |
| 45.36 | 43.58 | 48.35 | 59.49 | 42.49 | 43.99 | 47.32 | 58.65 | 41.31 | 42.85 | 62.29 | 46.33 | 47.71 | 57.85 | 58.96 | 41.75 |
| 39.28 | 14.8 | 10.91 | 14.61 | 6.51 | 5.2 | 17.09 | 19.66 | 14.68 | 14.14 | 16.93 | 10.74 | 10 | 14.48 | 13.94 | 4.83 |
| 18.1 | 1.81 | 4.39 | 4.39 | 7.81 | 3.5 | 4 | 4 | 7.6 | 3.01 | 5.66 | 8.59 | 5 | 8.59 | 5 | 8.17 |
| 10.23 | 7.03 | 1 | 2.47 | 5.43 | 0.63 | 7.05 | 7.4 | 8.84 | 7 | 2.53 | 5.46 | 0.82 | 5.91 | 2.41 | 5.4 |
| 23.37 | 6.83 | 5.92 | 8.49 | 6.02 | 7.4 | 3.79 | 7.17 | 3.94 | 5.84 | 6.32 | 2 | 4.75 | 6.4 | 7.72 | 4.87 |
| 37.38 | 3.41 | 3.11 | 6.39 | 3.26 | 2.72 | 3.41 | 6.54 | 3.54 | 3.05 | 6.39 | 3.26 | 2.72 | 6.46 | 6.21 | 2.88 |
| 38.04 | 3.05 | 9.34 | 1.89 | 5.06 | 3.05 | 9.56 | 2.79 | 5.46 | 3.68 | 9.25 | 10.38 | 9.56 | 4.9 | 2.79 | 5.46 |
| 38.09 | 18.3 | 5.73 | 6.05 | 5.46 | 8.6 | 17.82 | 17.93 | 17.74 | 18.94 | 4.4 | 3.56 | 7.54 | 4.05 | 7.78 | 7.34 |
| 9.22 | 9.75 | 4.57 | 15.58 | 5.53 | 4.22 | 8.98 | 17.39 | 9.51 | 8.81 | 15.11 | 4.02 | 1.84 | 15.43 | 15.01 | 3.62 |
| 22.21 | 4.8 | 4.8 | 5.13 | 10.2 | 5.2 | 0.2 | 1.81 | 9 | 2.01 | 1.8 | 9 | 2 | 9.18 | 2.69 | 9.22 |
| 37.29 | 1 | 2.47 | 3.06 | 7.82 | 0.63 | 2.53 | 3.1 | 7.84 | 0.82 | 3.84 | 8.16 | 2.41 | 8.36 | 3.01 | 7.8 |
| 29.15 | 6.26 | 4.57 | 4.75 | 4.02 | 1.8 | 7.32 | 7.44 | 7 | 6 | 6.08 | 5.53 | 4.2 | 5.69 | 4.4 | 3.6 |
| 15.27 | 2.86 | 2 | 5.73 | 2.51 | 3.05 | 3.05 | 6.17 | 3.41 | 3.82 | 5.82 | 2.72 | 3.22 | 6.02 | 6.26 | 3.56 |
| 23.2 | 2.6 | 4 | 4.2 | 4.6 | 5.8 | 4.77 | 4.94 | 5.28 | 6.36 | 5.8 | 6.1 | 7.05 | 6.23 | 7.16 | 7.4 |
| 23.32 | 11.63 | 10.72 | 11.01 | 14.71 | 11.07 | 5.81 | 6.32 | 11.63 | 6.44 | 16.49 | 10.72 | 4.6 | 11.01 | 5.23 | 11.07 |
| 32.35 | 6.79 | 11.32 | 9.62 | 7.17 | 9.62 | 9.34 | 7.18 | 3.22 | 7.18 | 11.56 | 9.62 | 11.56 | 7.54 | 9.9 | 7.54 |
| 20.03 | 3.33 | 2.06 | 6.65 | 2.28 | 4.2 | 2.97 | 6.99 | 3.13 | 4.72 | 6.48 | 1.72 | 3.93 | 6.55 | 7.44 | 4.05 |
| 3.05 | 10.51 | 4.12 | 8.14 | 4.72 | 3.93 | 9.93 | 12.16 | 10.19 | 9.85 | 7.38 | 3.22 | 1.89 | 7.73 | 7.27 | 2.97 |
| 5.06 | 2.06 | 4.12 | 3.93 | 1.72 | 2.6 | 4.39 | 4.2 | 2.28 | 3 | 5.52 | 4.24 | 4.66 | 4.05 | 4.49 | 2.78 |
| 5.02 | 0.2 | 0.4 | 5.4 | 3.2 | 0.4 | 0.45 | 5.4 | 3.21 | 0.45 | 5.41 | 3.22 | 0.57 | 6.28 | 5.41 | 3.22 |
| 2.11 | 2.28 | 3.06 | 6.43 | 1.9 | 1.52 | 3.72 | 6.77 | 2.84 | 2.61 | 7.07 | 3.5 | 3.31 | 6.65 | 6.55 | 2.28 |
| 2.14 | 6.72 | 8.07 | 5.49 | 7.5 | 9.32 | 7.21 | 4.12 | 6.56 | 8.59 | 6.08 | 7.94 | 9.68 | 5.3 | 7.67 | 9.21 |
| 14.01 | 10.55 | 4.87 | 5.56 | 8.32 | 6.25 | 9.43 | 9.81 | 11.6 | 10.22 | 2.91 | 6.85 | 4.08 | 7.35 | 4.88 | 7.89 |
| 14.19 | 3.16 | 4.28 | 3.05 | 6.72 | 5.11 | 3.85 | 2.41 | 6.46 | 4.75 | 3.76 | 7.07 | 5.56 | 6.4 | 4.68 | 7.6 |
| 14.25 | 11.68 | 7.24 | 7.47 | 8.54 | 7.73 | 9.23 | 9.41 | 10.29 | 9.62 | 2.15 | 4.67 | 2.91 | 5.02 | 3.44 | 5.39 |
| 25.12 | 8.49 | 7.69 | 5.73 | 2 | 5.34 | 11.33 | 10.1 | 8.55 | 9.88 | 9.44 | 7.77 | 9.21 | 13.76 | 7.64 | 5.44 |
| 12.13 | 6.9 | 3.45 | 3.76 | 5.1 | 5.56 | 12.61 | 6.21 | 7.1 | 7.44 | 1.71 | 3.85 | 4.44 | 4.12 | 4.68 | 5.81 |
| 13.24 | 12.53 | 4.33 | 7 | 4.02 | 3.86 | 12.24 | 13.42 | 12.13 | 12.08 | 6.46 | 3 | 2.78 | 6.26 | 6.16 | 2.28 |
| 25.07 | 8.81 | 4.42 | 9.01 | 2.04 | 6.01 | 9.84 | 12.59 | 9.02 | 10.65 | 10.02 | 4.83 | 7.96 | 9.22 | 10.82 | 6.32 |
| 7.08 | 4.32 | 4.65 | 8.51 | 4.22 | 5.66 | 2.24 | 7.47 | 1.08 | 3.93 | 7.67 | 2.04 | 4.29 | 7.41 | 8.32 | 3.82 |
| 8.36 | 4.75 | 4.56 | 10.93 | 9.31 | 8.1 | 2.16 | 10.16 | 8.4 | 7.03 | 10.07 | 8.29 | 6.91 | 12.93 | 12.09 | 10.65 |
| 3.31 | 7.69 | 8.59 | 3.61 | 3.94 | 3.74 | 10.35 | 6.8 | 6.99 | 6.87 | 7.8 | 7.96 | 7.86 | 1.61 | 1.02 | 1.89 |
| 31.3 | 4.44 | 2.47 | 11.22 | 2.67 | 1 | 5.01 | 12.03 | 5.11 | 4.47 | 11.45 | 3.54 | 2.53 | 11.5 | 11.23 | 2.72 |
| SUM: | 242.27 | 234.21 | 318.19 | 224.19 | 193.16 | 256.91 | 343.78 | 247.21 | 228.47 | 340.48 | 238.59 | 217.37 | 328.29 | 306.32 | 202.63 |



Fig. 1—Network with minimum covering connections in 6-dimensional space


Fig. 2-Tree with minimum covering distance in two-dimensional sense

## 7 Conclusions

In classical univariate or multivariate statistics, individual measurements are lost sight of in favour of estimated means and variances of samples of population. In multidimensional scaling, the identity of each point, each observation vector and its relationship to all other points are preserved and are central to the analysis. This provides a powerful tool for examining interrelationship among the individual observatories. There is a procedure for comparing the data of ground geomagnetic surveys with corresponding data of the nearest permanent observatory during geomagnetic quiet days. This is to
correct the measurement range of instruments and to eliminate abnormal values in the survey data. As a result of this study, it is expected that accurate determination of the solar quiet day field variation in terms of spanning distance can be used as a measure: to establish the interrelationship of measurements at one observatory to those at the others; to establish baselines from which magnetospheric disturbances are quantified; and for estimating the local anomalies while conducting ground geomagnetic surveys.

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## References

1 Sridharan M \& Ramasamy A M S, Multidimensional scaling technique for analysis of magnetic storms at Indian observatories, Proc Indian Aca. Sci (India), 4 (2002) pp 459-465.
2 Rastogi R G \& Patil A R, On certain aspects of daily variation of geomagnetic field at low latitudes, J Geomagn Geoelectr (Japan), 44 (1992) pp 495-503.
3 Alex S \& Rao D R K, Magnetospheric contribution to low latitude Sq variations, J Geomagn Geolectr (Japan), 47 (1995) pp 599-606.

4 Rangarajan G K, 'Best' estimates of the amplitude of diurnal and semidiurnal components of $\mathrm{Sq}(\mathrm{H})$ and their annual variations, Indian J Radio Space Phys, 4 (1975) pp 46-49.
5 Alex S, Kadam B D \& Rao D R K, Ionospheric current system on days of low equatorial $\Delta \mathrm{H}$, J Atmos Sol-Terr Phys (UK), 3 (1998) pp 371-379.

6 Rangarajan G K \& Dhar Ajay, Response of the Sq and equatorial electrojet and variations to the north-south asymmetry in geomagnetic activity, J Geomagn Geolectr (Japan), 44 (1992) pp 899-908.
7 Yacob A, Latitudinal profile in India of $\mathrm{Sq}(\mathrm{H})$ range and of its prominent periodicities, Pure Appl Geophys (Switzerland), 113 (1975) pp 601-608.
8 Carrol J D, Models and methods for multidimensional analysis of preferential choice (or other dominance) data in similarity and choice, edited by E D Lantermann \& H Feger, (Hans Huber, Bern), 1980, pp 234-289.

9 Encyclopedia of Bio-statistics, edited by P Armitage \& T Cotton, (Wiley, New York), 1998, 5.
10 Thompson H K Jr \& Woodbury M A, Clinical data representation in multidimensional space, Comput Biomed Res (USA), 3 (1970) pp 58-73.
11 Yacob A \& Sen A K, On quiet day maximum and minimum range in H, Pure Appl Geophys (Switzerland), 112 (2) (1974) pp 464-471.
12 Sridharan M, Gururajan N \& Ramasasmy A M S, Fuzzy clustering analysis to study geomagnetic coastal effects, Ann Geophys (France), 23 (2005) pp 1157-1163.

